

START

$i = 1$

NEW PHOTON
sample a viewing direction (θ, ϕ) from the antenna response function.

$i = i + 1$

SCATTERING
sample a new incident direction $(\theta_{inc}, \phi_{inc})$ according to
$$g(\theta_{inc}, \phi_{inc}) = \frac{Z_{11}(\theta_{scat}, \phi_{scat}, \theta_{inc}, \phi_{inc}) \sin(\theta_{inc})}{K_{11}(\theta_{scat}, \phi_{scat}) - K_{a1}(\theta_{scat}, \phi_{scat})}$$

Calculate the matrix $\mathbf{Q}_k = \mathbf{Q}_{k-1} \mathbf{q}_k$, where
$$\mathbf{q}_k = \frac{\sin(\theta_{inc})_k \mathbf{O}(\mathbf{s}_k, \mathbf{s}_{k-1}) \mathbf{Z}(\mathbf{n}_{k-1}, \mathbf{n}_k)}{g(\Delta s) g(\theta_{inc}, \phi_{inc}) \tilde{\omega}}$$

and $\mathbf{Q}_0 = \mathbb{1}$.

$k = 0$

Sample a new path length, Δs along the new direction using the PDF
$$g(\Delta s) = \tilde{k} \tilde{O}_{11}(\Delta s)$$

$k = k + 1$

$k = k + 1$

SURFACE REFLECTION
Get new incident direction \mathbf{n}_k from surface scheme. Calculate the matrix $\mathbf{Q}_k = \mathbf{Q}_{k-1} \mathbf{q}_k$, where
$$\mathbf{q}_k = \frac{\mathbf{O}(\mathbf{u}_k, \mathbf{s}_k) \mathbf{R}(\mathbf{n}_{k-1}, \mathbf{n}_k)}{O_{11}(\mathbf{u}_k, \mathbf{s}_k) R_{11}}$$

and $\mathbf{Q}_0 = \mathbb{1}$.

NO
 $r > \tilde{\omega}$?
YES

INSIDE ATMOSPHERE
where does the path end?
SURFACE
TOP OF ATMOSPHERE

NO
 $r > R_{11}$?
YES

EMISSION
$$\mathbf{I}^i(\mathbf{n}, \mathbf{s}_0) = \frac{\mathbf{Q}_k \mathbf{O}(\mathbf{s}_{k+1}, \mathbf{s}_k) \mathbf{K}_a(\mathbf{n}_k, \mathbf{s}_{k+1}) I_b(T, \mathbf{s}_{k+1})}{g(\Delta s) (1 - \tilde{\omega})}$$

TOP OF ATMOSPHERE
$$\mathbf{I}^i(\mathbf{n}, \mathbf{s}_0) = \frac{\mathbf{Q}_k \mathbf{O}(\mathbf{u}_k, \mathbf{s}_k) \mathbf{I}_{space}(\mathbf{n}_k, \mathbf{u}_k)}{O_{11}(\mathbf{u}_k, \mathbf{s}_k)}$$

SURFACE EMISSION
$$\mathbf{I}^i(\mathbf{n}, \mathbf{s}_0) = \frac{\mathbf{Q}_k \mathbf{O}(\mathbf{u}_k, \mathbf{s}_k) \mathbf{I}_{surf}(\mathbf{n}_k, \mathbf{u}_k)}{O_{11}(\mathbf{u}_k, \mathbf{s}_k) (1 - R_{11})}$$

FINISH
$$\mathbf{I}(\mathbf{n}, \mathbf{s}_0) = \frac{1}{N} \sum_{i=1}^N \mathbf{I}^i(\mathbf{n}, \mathbf{s}_0).$$

YES
 $i = N$?
NO

